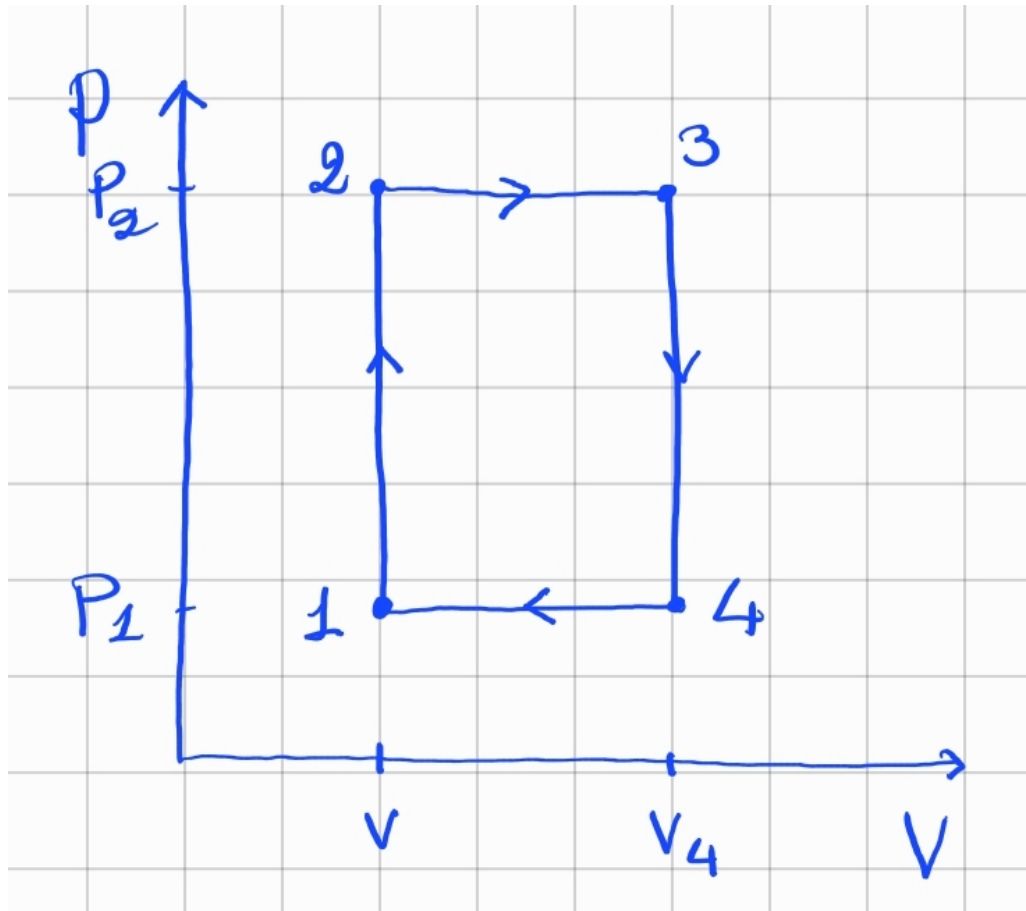


Exercise #1

due date: October 24 2022

a) Consider the following thermodynamic cycle for a perfect gas:



- Draw the cycle in the T-S plane.
- Calculate the total work exerted by the system (W).
- Calculate the total heat exchanged by the system (Q).
- Calculate the efficiency $\eta = \{W\} / \{Q_{\text{abs}}\}$ where Q_{abs} is the absorbed heat.

In the following you can alternatively choose b1) or b2).

b1) Read the notes about the Kac ring model:

- which set of variables describes a *microscopic* state?

- which set of variables describes the *macroscopic* state?
- write a code to calculate the number of black and white point (you can also do it considering a small size say $N=4$ and doing the evolution by hand...)
- compare the output of the code with the "molecular-chaos" solution given in the notes and discuss the results.

b2) Read the notes about the Logistic map:

- write a code to calculate the map evolution and the Lyapunov exponent.
- discuss the results in the parameters space described in the note discussing the local stability and the Lyapunov exponent.
- When the system is chaotic the time average of y converge to a time-independent value? Is this value independent on initial data?

c1) Consider only one one-dimensional classical harmonic oscillator

- write the Hamilton equation and *plot* a typical trajectory in the phase space
- is the system chaotic?

c2) now consider an ensemble made of replicas of the previous case i.e. one-dimensional classical harmonic oscillator with same ω and mass

- write the Liouville's evolution for an ensemble of such systems using momenta and position as variables
- consider an *isoenergetic* ensemble of oscillators (all osc. have energy= E). This ensemble starts with random phases between ϕ_0 and $\phi_0 + \Delta$. In such conditions evaluate $\langle x(t) \rangle$. Does it tends to a constant value? Is the system ergodic? Is the system mixing?

Last updated 2022-10-30 15:50:42 CET